

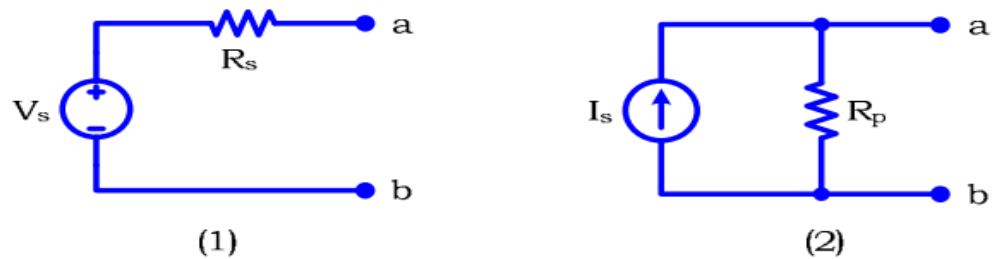
# Lecture 07: Source Transformation

## Source Transformation:

Given an ideal voltage source  $V_s$  in series with a resistor  $R_s$ .

⇓ (can we replace them with)

An ideal current source  $I_s$  in parallel with a resistor  $R_p$ ?



**Figure 1**

Connect the *same* load resistor  $R_L$  across terminal “a-b” in both circuits.

If circuits “1” and “2” are *equivalent*  $\Rightarrow I_1 = I_2$  &  $V_1 = V_2$

$$\text{Circuit “1”} \Rightarrow I_1 = \frac{V_s}{R_{eq}} = \frac{V_s}{R_s + R_L} \quad (1)$$

$$\text{Circuit “2”} \Rightarrow I_2 = \frac{R_p}{R_p + R_L} I_s \quad (2) \quad (\text{CDR is used})$$

$$I_1 = I_2 \Rightarrow \frac{V_s}{R_s + R_L} = \frac{R_p I_s}{R_p + R_L} \quad (3)$$

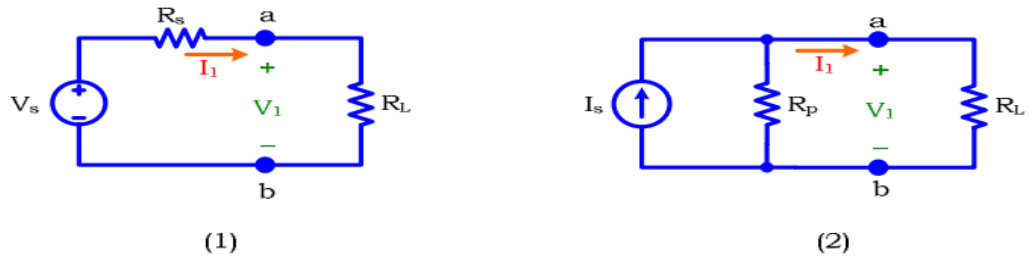
If we choose  $R_p = R_s \Rightarrow V_s = I_s R_p = I_s R_s$

$$\therefore R_s = R_p \quad \& \quad V_s = I_s R_s$$

⇓

$$V_s \text{ in series with } R_s \quad \Leftrightarrow \quad I_s \text{ in parallel with } R_s$$

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**Figure 2**

The above conversion is called *Source Transformation (ST)*.

Circuits (1) & (2) are *equivalent*. However, they are *not the same*.

When *any load* is connected to terminals “a” & “b” of circuits (1) & (2)



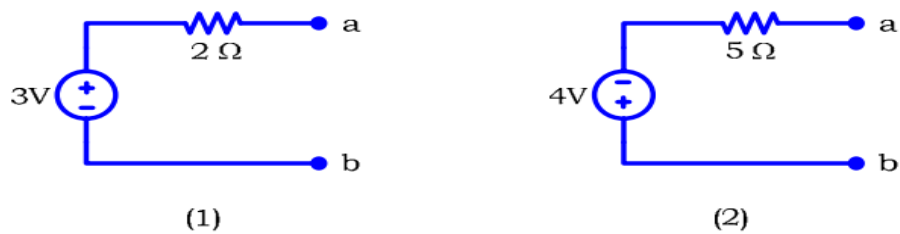
Load *cannot distinguish* between the two circuits.

Circuits (1) & (2) are *equivalent* from the *outside* when accessed from terminals “a” & “b”.

Circuits (1) & (2) are *different* from the *inside*.

## Example 1:

Covert the following circuits using ST.



**Figure 3**

Solution:

Circuit (1):

$$R_p = R_s = 2\Omega$$

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$$I_s = \frac{V_s}{R_s} = \frac{3}{2} = 1.5A$$

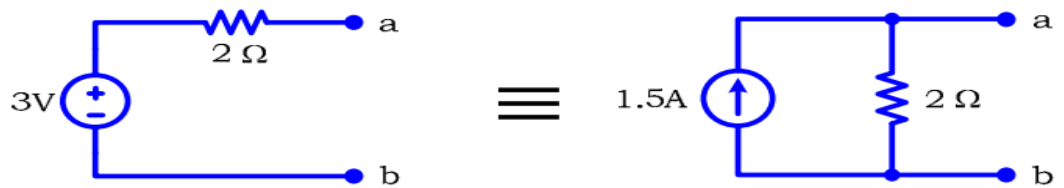


Figure 4

Circuit (2):

$$R_p = R_s = 5\Omega$$

$$I_s = \frac{V_s}{R_s} = \frac{4}{5} = 0.8A \text{ (downwards. Why?)}$$



Figure 5

## Example 2:

Convert the following circuits using ST.

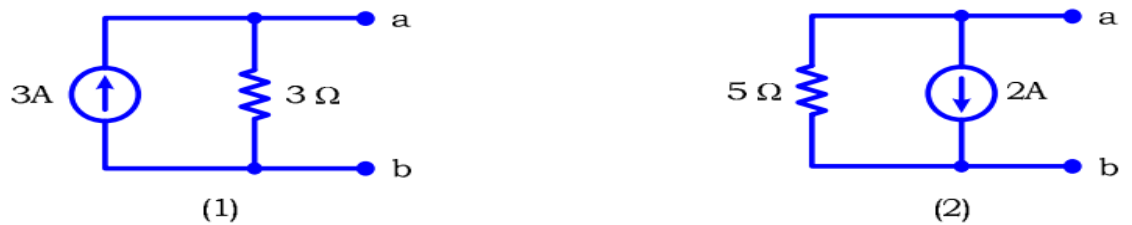


Figure 6

Solution:

Circuit (1):

$$R_s = R_p = 3\Omega \quad \& \quad V_s = R_s I_s = 3(3) = 9V$$

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Figure 7

Circuit (2):

$$R_s = R_p = 5\Omega$$

$$\& \quad V_s = R_s I_s = 5(2) = 10V \quad (\text{upper voltage polarity is negative. Why?})$$



Figure 8

You need to be careful when using ST, as we will see in the next example.

### Example 3:

Covert the following circuits using ST.

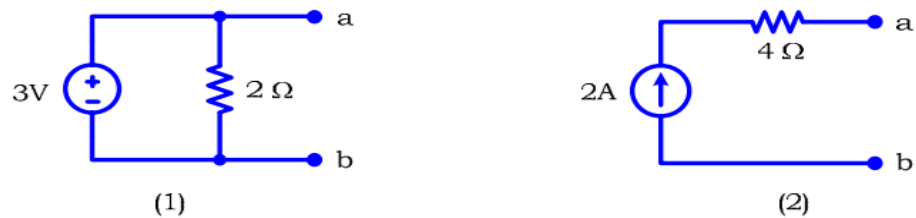


Figure 9

Solution:

Circuit (1):

A resistor *in parallel* with a voltage source (*not in series*)  $\Rightarrow$  ST *does not* apply.

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A resistor in parallel with a voltage source  $\Rightarrow$  equivalent to a voltage source.

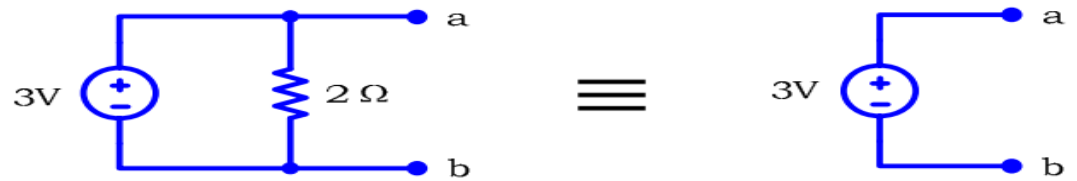


Figure 10

Circuit (2):

A resistor *in series* with a current source (*not in parallel*)  $\Rightarrow$  ST does not apply.

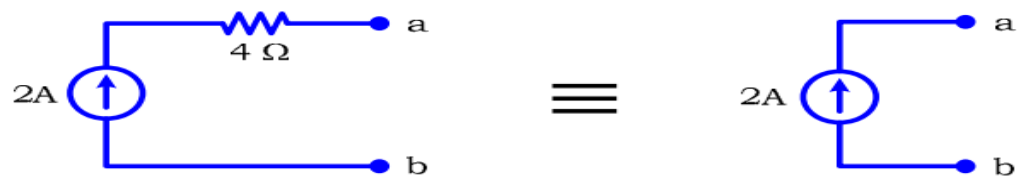


Figure 11

A resistor in series with a current source  $\Rightarrow$  equivalent to a current source.

### Example 4:

Use ST to calculate:

- a)  $i_1$
- b)  $i_2$

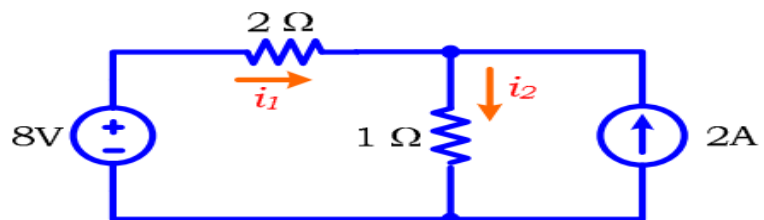


Figure 12

Solution:

It is a good idea to first label some points on the circuit.

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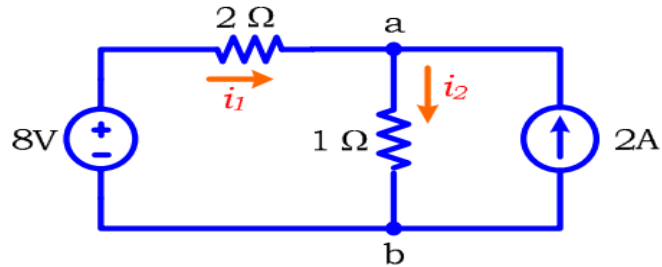


Figure 13

Apply ST to the  $2A$  &  $1\Omega$  combination  $\Rightarrow V = IR = 2(1) = 2V$

Notice that  $i_2$  cannot be drawn. It disappears. Why?

The current through the  $1\Omega$  of the *transformed* circuit is *not*  $i_2$ . Why?

Reason:  $R_p = R_s$  means the two resistors have the *same* value. It *does not* mean we have the same resistor!!

$\therefore 2\Omega$  &  $1\Omega$  in series  $\Rightarrow$  current through the  $1\Omega$  of the *transformed* circuit is  $i_1$ .

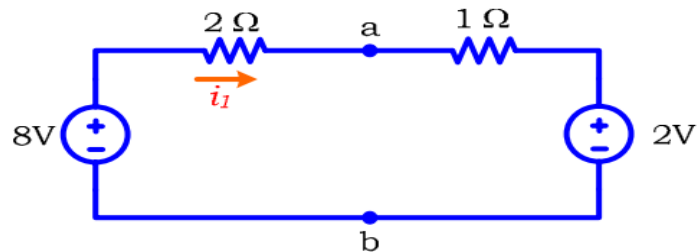


Figure 14

$2\Omega$  &  $1\Omega$  in series  $\Rightarrow 3\Omega$

$8V$  &  $2V$  in series  $\Rightarrow 8 - 2 = 6V$

a)  $i_1 = \frac{6}{3} = 2A$

b) KCL at node “a” (of the original circuit)  $\Rightarrow i_2 = i_1 + 2 = 2 + 2 = 4A$

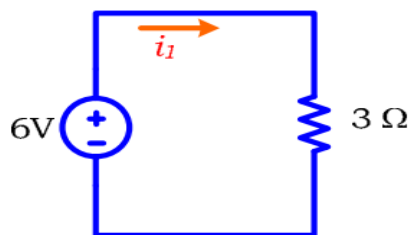


Figure 15

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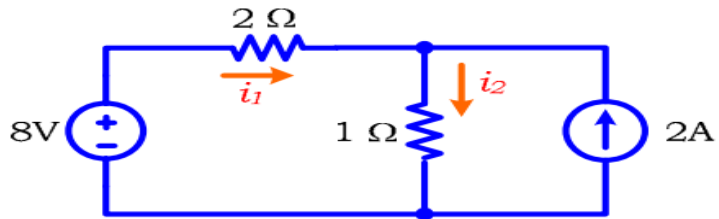


Figure 12

### Example 5:

Use ST to calculate  $V$ .

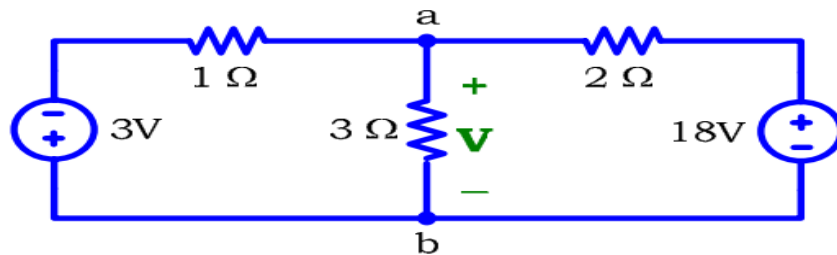


Figure 16

Solution:

Apply ST to ( $3V$  in series with  $1\Omega$ ) & ( $18V$  in series with  $2\Omega$ )

$$I_{s1} = \frac{3}{1} = 3A \quad \& \quad I_{s2} = \frac{18}{2} = 9A$$

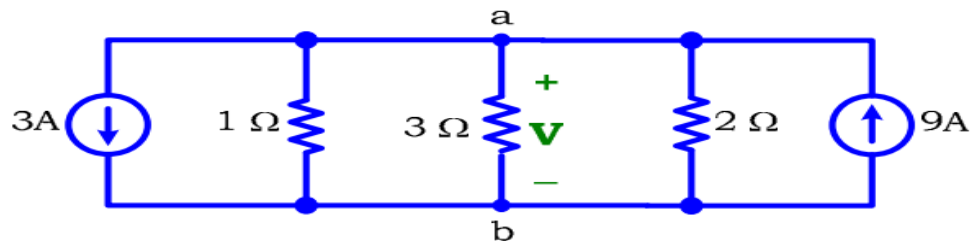


Figure 17

$$1\Omega \parallel 3\Omega \parallel 2\Omega \Rightarrow R_{eq} = \frac{1}{1 + \frac{1}{3} + \frac{1}{2}} = 0.545\Omega$$

$$3A \parallel 9A \Rightarrow I_{eq} = 9 - 3 = 6A$$

$$\therefore V = I_{eq} R_{eq} = 6(.545) = 3.273V$$

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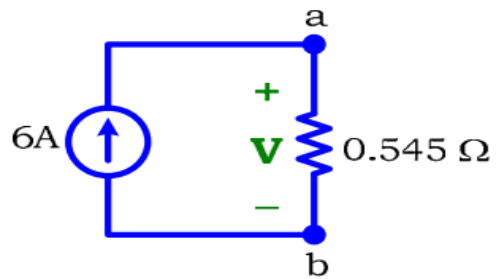


Figure 18

**Example 5:** Using ST, calculate:

a)  $i_1$

b)  $i_2$

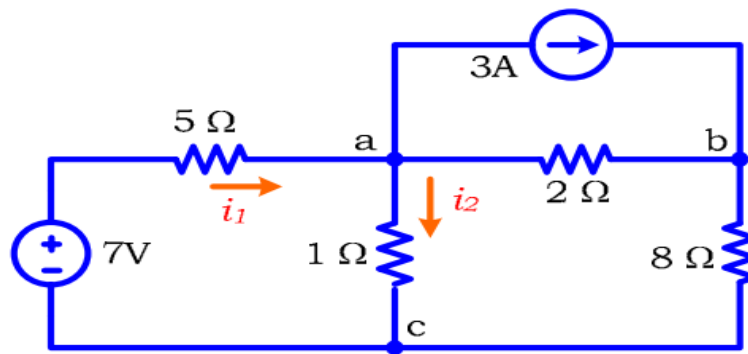


Figure 19

Solution:

$$\text{ST} \Rightarrow V = 3 \times 2 = 6V$$

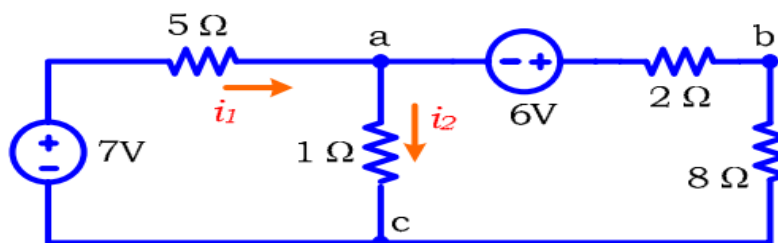


Figure 20

$$2\Omega \parallel 8\Omega \Rightarrow 10\Omega$$

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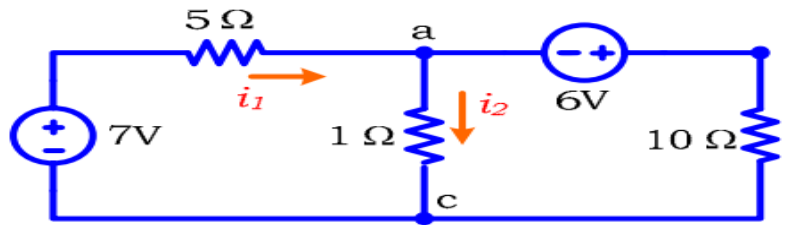


Figure 21

$$ST \Rightarrow I = \frac{6}{10} = 0.6A$$

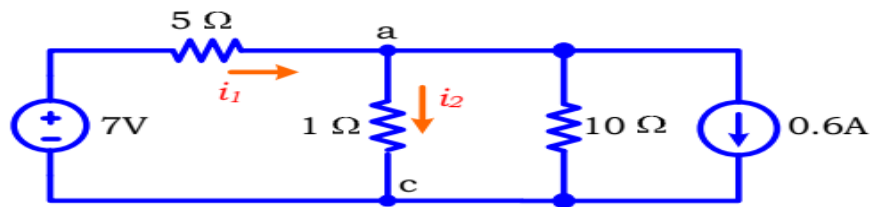


Figure 22

$$1\Omega \parallel 10\Omega \Rightarrow \frac{10 \times 1}{10 + 1} = \frac{10}{11} = 0.909\Omega$$

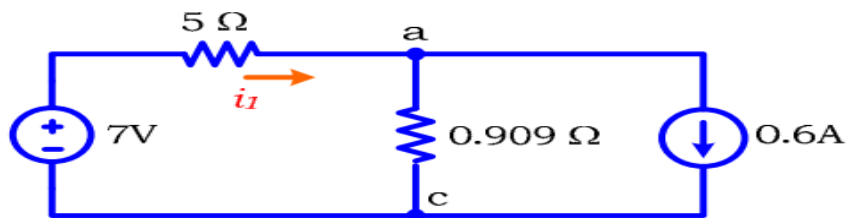


Figure 23

$$ST \Rightarrow V = 0.909 \times 0.6 = 0.545V$$

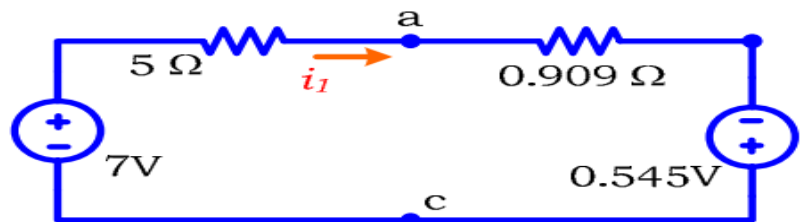


Figure 24

$$R_{eq} = 5 + 0.909 = 5.909\Omega \quad \& \quad V_{eq} = 7 + 0.545 = 7.545V$$

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a)  $\therefore i_1 = \frac{7.545}{5.909} = 1.277 A$

b) KVL (in the original circuit)  $\Rightarrow -7 + 5i_1 + 1i_2 = 0 \Rightarrow -7 + 5(1.277) + 1i_2 = 0 \Rightarrow i_2 = 0.615 A$

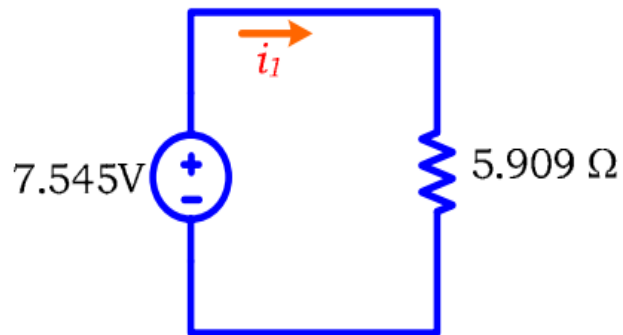


Figure 25

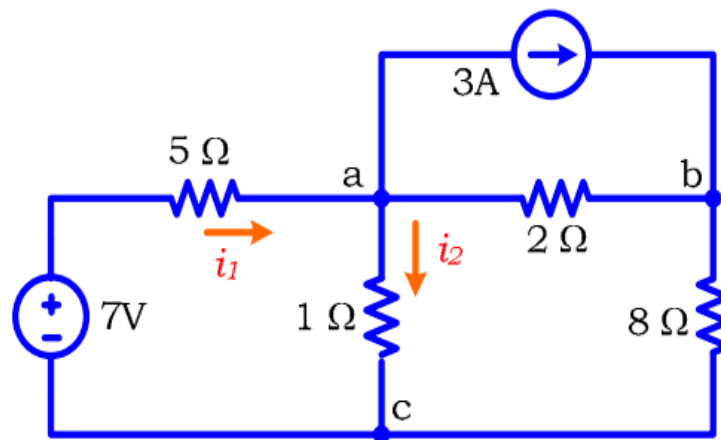


Figure 19