

# Lecture 13: Mesh Analysis - Introduction

## Definition of Mesh

The circuit contains four windows (meshes).

A mesh is simply a *window* in an electric circuit

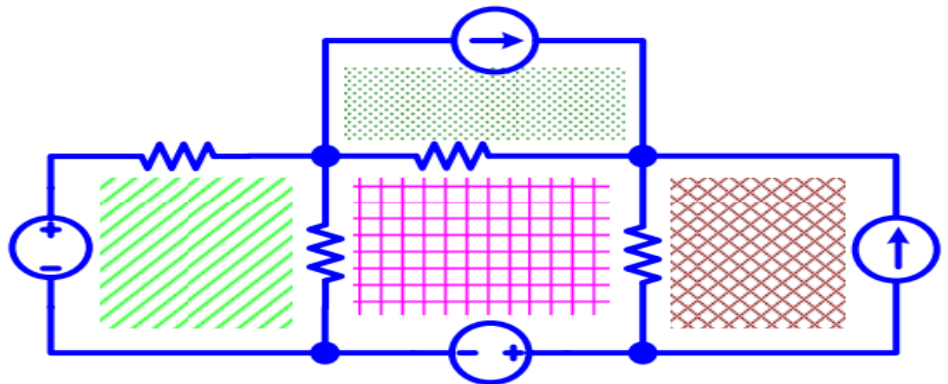


Figure 1

## Currents through Elements & Mesh Currents:

The currents  $i_a$ ,  $i_b$ ,  $i_c$  are currents through elements

$$\text{KCL at node 1} \Rightarrow i_a = i_b + i_c \Rightarrow i_b = i_a - i_c$$

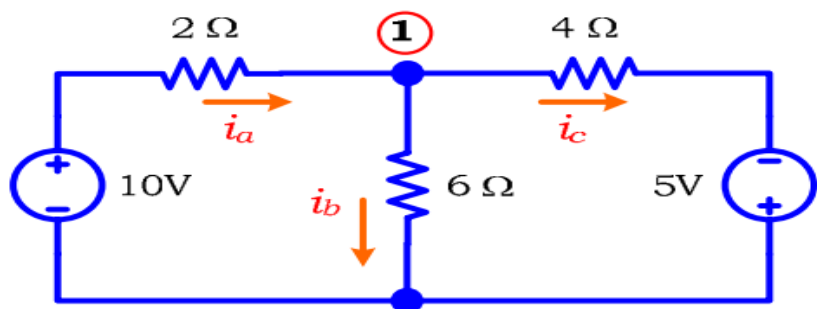


Figure 2

The *imaginary* currents  $i_1$  &  $i_2$  are *mesh* currents

We imagine  $i_1$  to circulate around mesh 1 (CW)

We imagine  $i_2$  to circulate around mesh 2 (also CW)

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$$i_a = i_1 \quad (\text{because only mesh current } i_1 \text{ goes through } 2\Omega \text{ and } 10V)$$

$$i_c = i_2 \quad (\text{because only mesh current } i_2 \text{ goes through } 4\Omega \text{ and } 5V)$$

$$i_b = i_a - i_c = i_1 - i_2 \quad (\text{two mesh currents } i_1 \text{ \& } i_2 \text{ go through } 6\Omega \text{ in opposite directions})$$

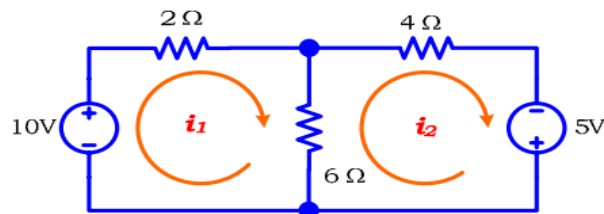


Figure 3

### Example 1:

Express the currents through elements (CTE)  $i_x$ ,  $i_y$ ,  $i_z$ ,  $i_w$  in terms of mesh currents (MC)  $i_1$  &  $i_2$ .

Solution:

$$i_x = i_1$$

$$i_y = -i_3$$

$$i_z = i_1 - i_2$$

$$i_w = i_3 - i_1$$

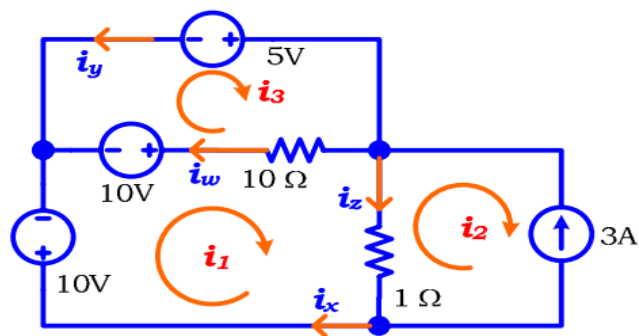


Figure 4

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We know all MC  $\Rightarrow$  We know all CTE

Number of MC  $\leq$  Number of CTE

## Mesh Analysis (without Current Sources):

The Mesh Analysis procedure for circuits *without* current sources will be considered first.

We will learn the *basic* Mesh Analysis procedure through a simple example.

### Example 2:

Calculate the mesh currents  $i_1$  &  $i_2$ .

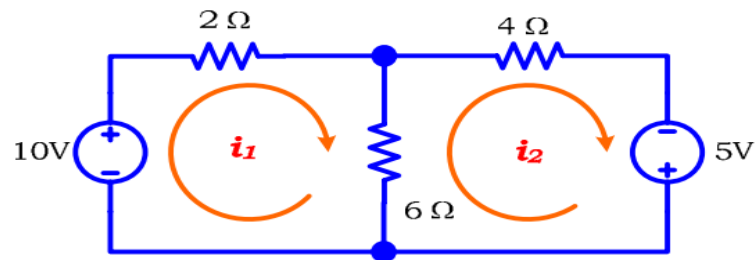


Figure 5

Solution:

Procedure:

1- KVL around mesh 1  $\Rightarrow -10 + V_a + V_b = 0$

2- Ohm's Law  $\Rightarrow -10 + 2i_a + 6i_b = 0$

3- KCL  $\Rightarrow -10 + 2i_1 + 6(i_1 - i_2) = 0$  [CTE are expressed in terms of MC]

4- Simplify  $\Rightarrow 8i_1 - 6i_2 = 10$  (1)

Repeat the same procedure for the remaining meshes:

1- KVL around mesh 2  $\Rightarrow -V_b + V_c - 5 = 0$

2- Ohm's Law  $\Rightarrow -6i_b + 4i_c - 5 = 0$

3- KCL  $\Rightarrow -6(i_1 - i_2) + 4i_2 - 5 = 0$  [CTE are expressed in terms of MC]

4- Simplify  $\Rightarrow -6i_1 + 10i_2 = 5$  (2)

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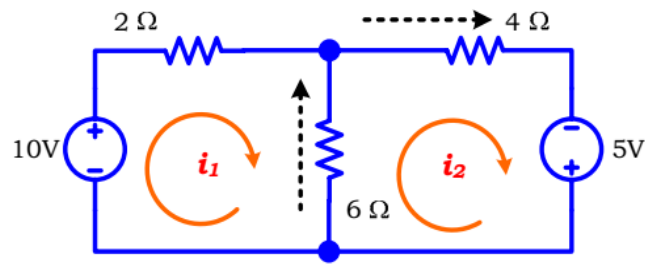


Figure 8

**Example 3:** Calculate the mesh currents  $i_1$  &  $i_2$  &  $i_3$

Solution:

$$\text{Mesh 1: } \Rightarrow 4i_1 - 8 + 6(i_1 - i_2) = 0 \quad \Rightarrow \quad 10i_1 - 6i_2 = 8 \quad (1)$$

$$\text{Mesh 2: } \Rightarrow 6(i_2 - i_1) + 8(i_2 - i_3) + 12 = 0 \quad \Rightarrow \quad -6i_1 + 14i_2 - 8i_3 = -12 \quad (2)$$

$$\text{Mesh 3: } \Rightarrow 2i_3 + 8(i_3 - i_2) + 8 = 0 \quad \Rightarrow \quad -8i_2 + 10i_3 = -8 \quad (3)$$

$$\text{Solving (1) \& (2) \& (3) } \Rightarrow i_1 = -1.24\text{A} \ \& \ i_2 = -3.40\text{A} \ \& \ i_3 = -3.52\text{A}$$

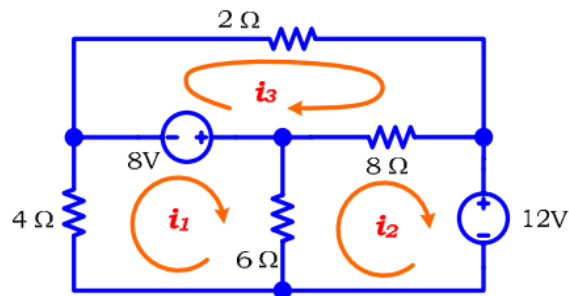


Figure 9