

**FINAL EXAMINATION**

**OBSERVE SILENCE IN THE EXAM ROOM**

**SECTION A**

**QUESTION 1. (20 Marks)**

Solve the initial value problem.

$$y^{(4)} = -\sin t + \cos t; \quad y'''(0) = 7, \quad y''(0) = y'(0) = -1, \\ y(0) = 0$$

**QUESTION 2. (20 Marks)**

Given the velocity,

$$v = \frac{ds}{dt} = 32t - 2,$$

and the initial position of the body as  $s(1/2) = 4$ . Find the body's position at time  $t$ .

**QUESTION 3. (20 Marks)**

Given the acceleration,  $a = d^2s/dt^2 = -4\sin 2t$ , initial velocity  $v(0) = 2$ , and the initial position of the body as  $s(0) = -3$ . Find the body's position at time  $t$ .

**SECTION B**

**QUESTION 4. (10 Marks)**

Solve the initial value problem.

$$\frac{dy}{dx} = 10 - x, \quad y(0) = -1$$

**QUESTION 5. (10 Marks)**

Solve the initial value problem.

$$\frac{dy}{dx} = 9x^2 - 4x + 5, \quad y(-1) = 0$$

**QUESTION 6. (10 Marks)**

Solve the initial value problem.

$$\frac{ds}{dt} = \cos t + \sin t, \quad s(\pi) = 1$$

**QUESTION 7. (10 Marks)**

Solve the initial value problem.

$$\frac{d^2y}{dx^2} = 2 - 6x; \quad y'(0) = 4, \quad y(0) = 1$$