

Image Enhancement in Spatial Domain(Point Processing)



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Outline of Lecture2

- ❑ Introduction
- ❑ Arithmetic Operations
- ❑ Logic Operations
- ❑ Histogram Stretching
- ❑ Histogram Equalization
- ❑ Histogram Matching
- ❑ Lookup Tables

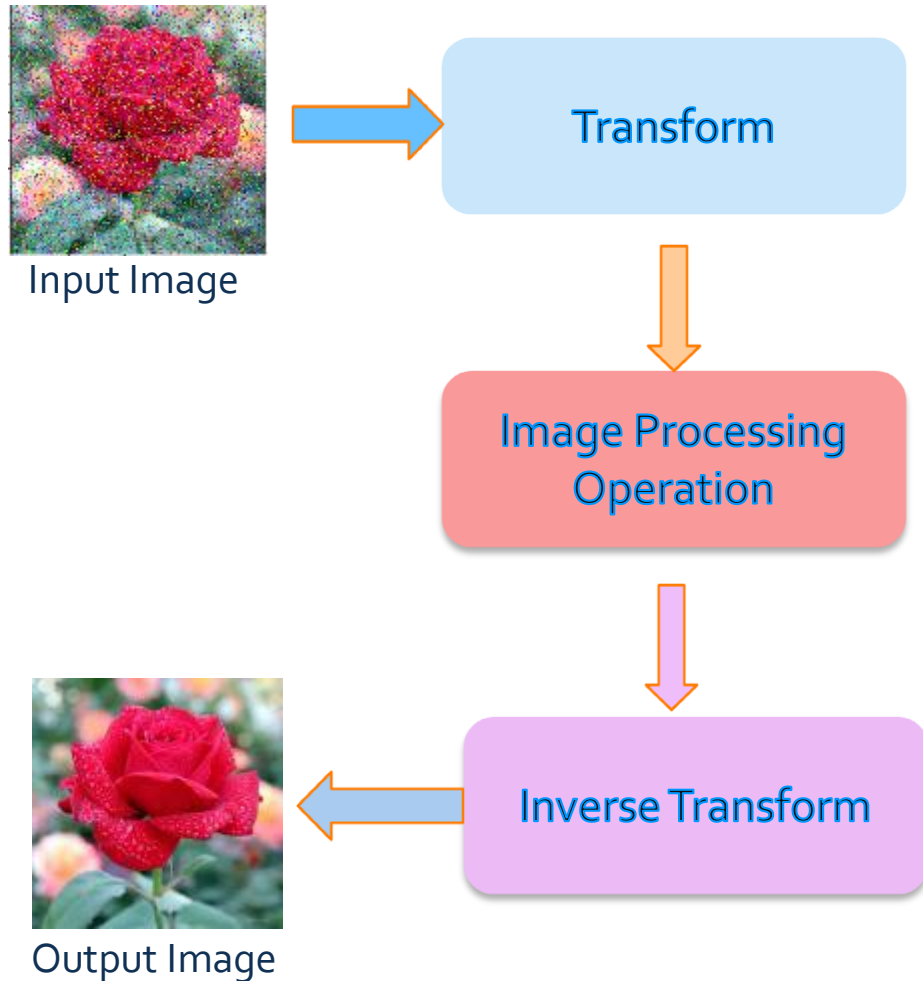
Introduction

- ❑ Any image processing operation **transforms the grey values** of the pixels.
- ❑ However, image processing operations may be divided into **three classes** based on the information required to perform the transformation. They are:
 - **Transforms**
 - **Neighbourhood processing**
 - **Point operations**

Transforms

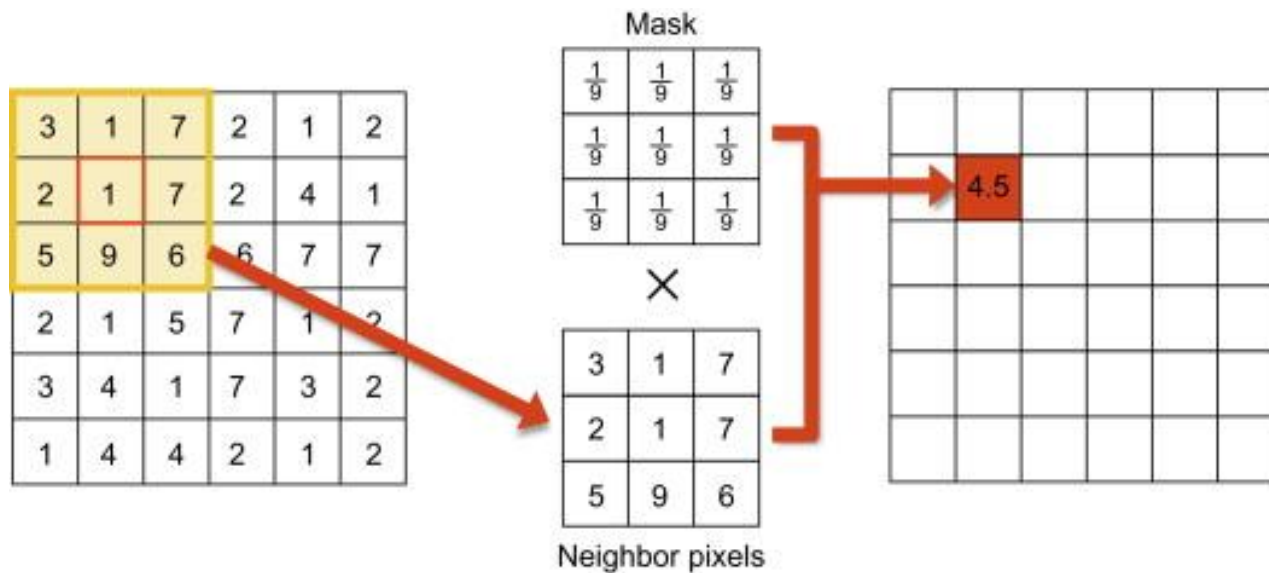
- ❑ A transform represents the pixel values in some other, but **equivalent form**.
- ❑ Transforms allow for some very **efficient and powerful** algorithms.
- ❑ In using a transform, the entire image is processed as a **single large block**.

Steps in Transform Processing



Neighbourhood processing

- To change the grey level of a given pixel we need only know the value of the grey levels in a small **neighbourhood** of pixels around the given pixel.



Neighbourhood processing

Point operations

- ❑ A pixel's grey value is changed **without any knowledge of its surrounds.**
- ❑ Although point operations are the **simplest**, they contain some of the most **powerful** and **widely** used of all image processing operations.
- ❑ They are especially **useful** in image pre-processing, where an image is required **to be modified before the main job** is attempted.

Point operations

- ❑ Some point operations are
 - Arithmetic operations
 - Logic Operations
 - Histogram stretching (Contrast stretching)
 - Histogram equalization
 - Histogram Matching
 - Lookup tables

Arithmetic operations

- Arithmetic operations act by applying a **simple function** to each grey value in the image. Thus $f(x)$ is a function which **maps** the range **0 ...255** onto **itself**. Simple functions include **adding** or **subtract** a constant value to each pixel or **multiplying** each pixel by a constant in order to ensure that the results are integers in **the 0...255 range**.

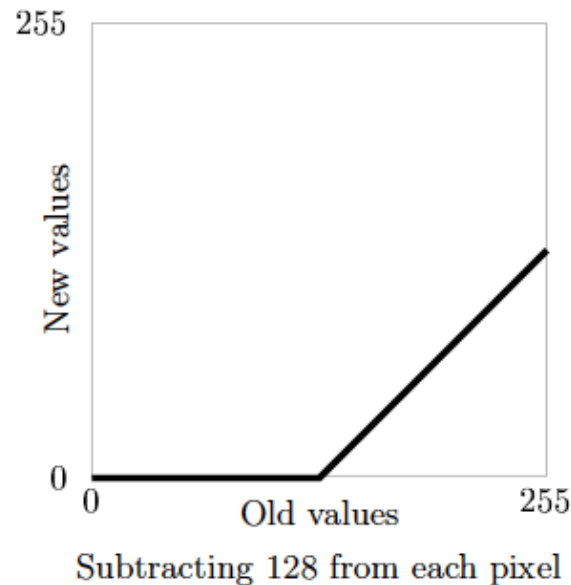
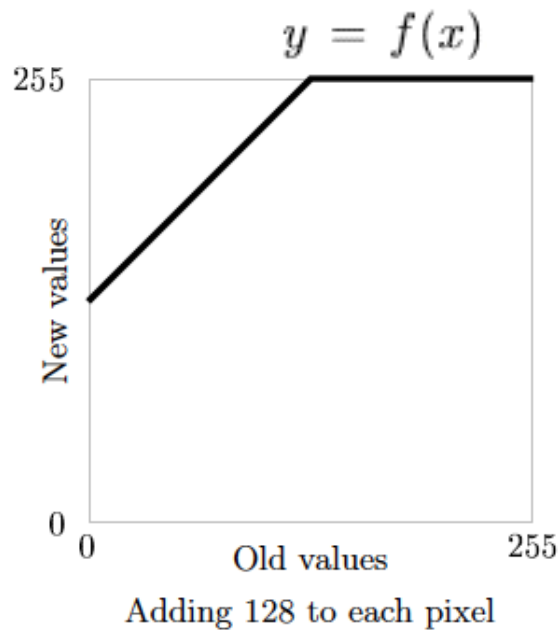
$$y = f(x), \quad y = x \pm c, \quad y = Cx$$

- We can do this by first **rounding the result** to obtain an integer, and then "**clipping**" the values by setting:

$$y \leftarrow \begin{cases} 255 & \text{if } y > 255 \\ 0 & \text{if } y < 0 \end{cases}$$

Arithmetic operations

- in general adding a constant will lighten an image, and subtracting a constant will darken it.



Notice that when we add 128, all grey values of 127 or greater will be mapped to 255. And when we subtract 128, all grey values of 128 or less will be mapped to 0.

Adding and subtracting a constant

Image Addition



Image1



Image2



Addition of two images

```
## Addition of two images##  
from PIL.ImageChops import add, subtract, multiply, difference  
from PIL import Image  
im1 = Image.open("images/image1.jpg")  
im2 = Image.open("images/image2.jpg").convert('RGB').resize((im1.width, im1.height))  
add(im1, im2).show()
```

Image Addition (cont.)



Image1



Image2



Addition of two images

Arithmetic operations on an image: addition

Image Addition (cont.)



Image1



Image2



Addition of two images

Arithmetic operations on an image: addition

Implementing pixel addition/subtraction by Python commands

```
import matplotlib.pyplot as plt
import skimage.io as io
import numpy as np

img=io.imread('images/rice.tif');
plt.figure()
io.imshow(img)
img=np.float64(img)
img1=np.uint8(np.clip(img+128,0,255))
plt.figure()
io.imshow(img1)
img2=np.uint8(np.clip(img-128,0,255))
plt.figure()
io.imshow(img2)
```



Original Image



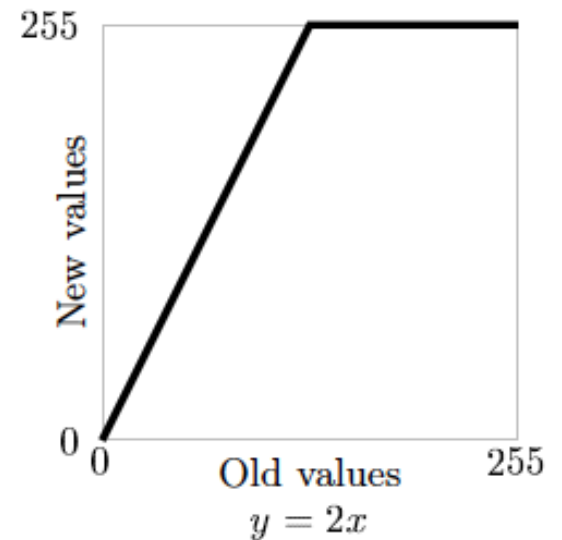
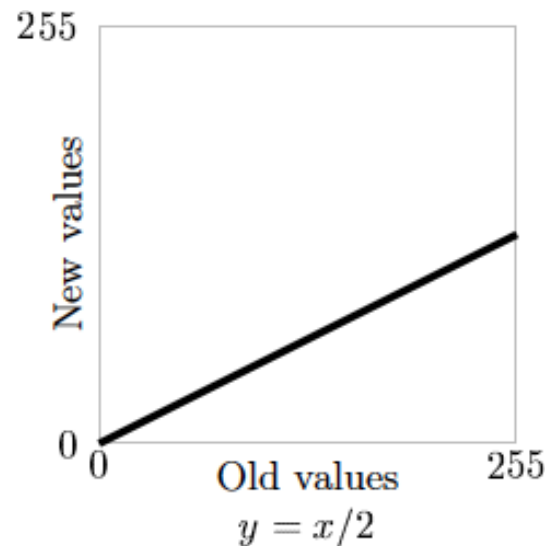
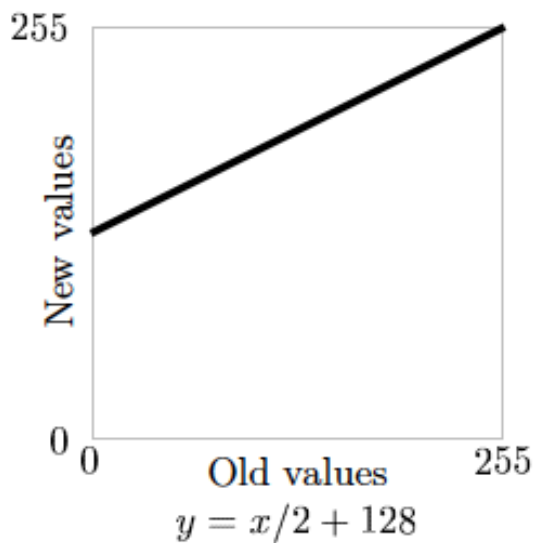
Adding 128



Subtracting 128

Implementing pixel multiplication by Python commands

- ❑ Arithmetic operations on image are performed by dividing and multiplying by 2 to each pixel values.



Implementing pixel multiplication by Python commands (cont.)



original image



$y = x/2$



$y = 2x$

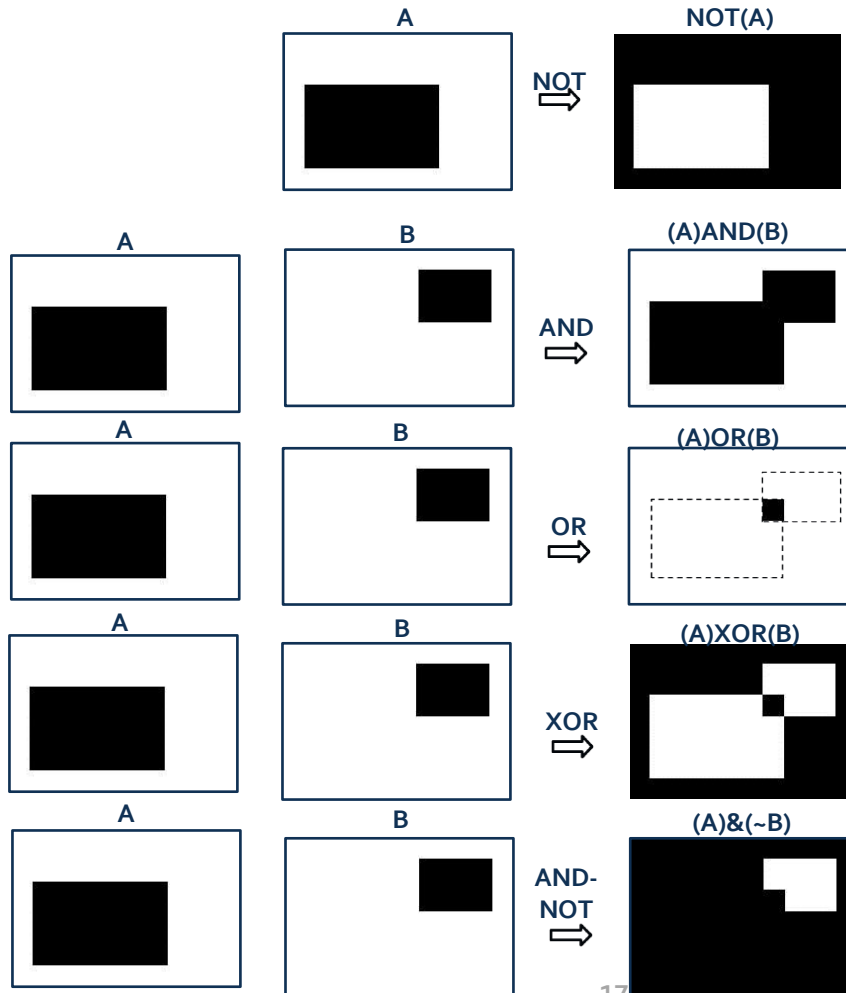


$y = x/2 + 128$

```
img=io.imread('images/jasmine.jpg');  
plt.figure()  
io.imshow(img)  
img=np.float64(img)  
img1=np.uint8(np.clip((img/2),0,255))  
plt.figure()  
io.imshow(img1)  
img2=np.uint8(np.clip((img*2),0,255))  
plt.figure()  
io.imshow(img2)  
img3=np.uint8(np.clip((img/2)+128,0,255))  
plt.figure()  
io.imshow(img3)
```

Arithmetic operations on an image: multiplication and division

Logic Operations



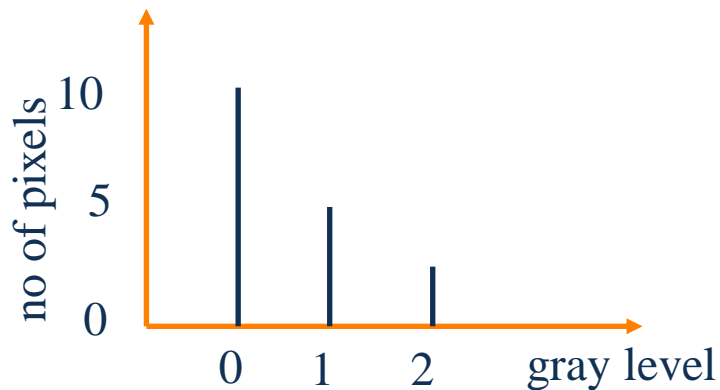
Some logic operations between binary images. Black represents binary 0s and white binary 1s.

Histograms

- Given a greyscale image, its **histogram** consists of the histogram of its grey levels; that is, a graph indicating the **number of times each grey level occurs** in the image.

0	0	0	2
0	1	1	0
0	1	1	0
2	0	0	0

Image with **gray level 3**

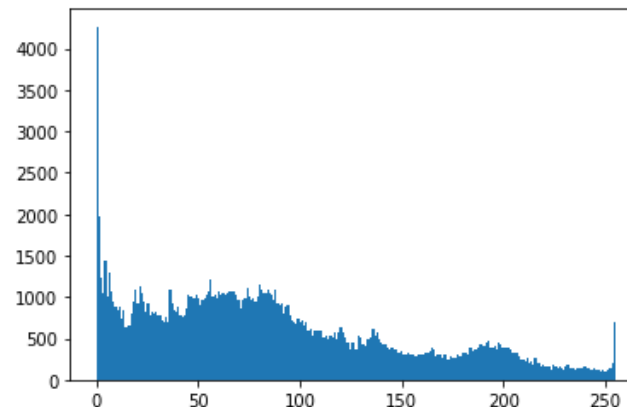


Histogram of the image

Histograms (cont.)

- We can view the histogram of an image in Python by using the `plt.hist` function:

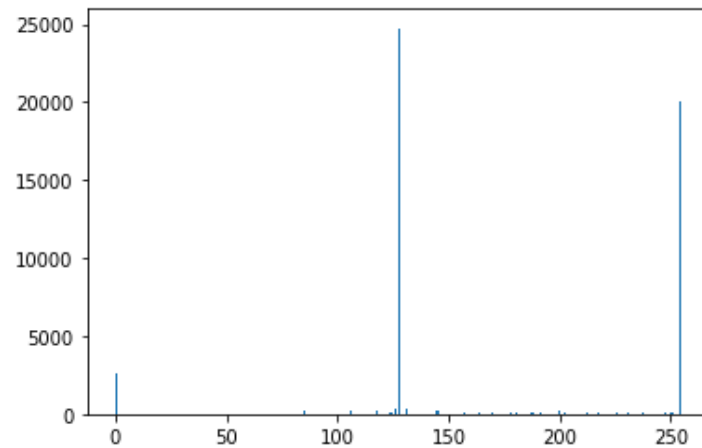
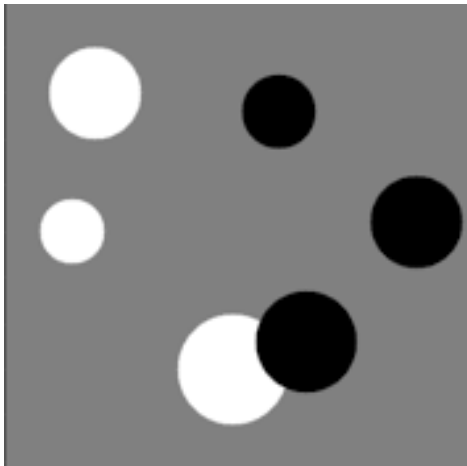
```
import matplotlib.pyplot as plt
img=io.imread('images/redrose.jpg');
plt.figure()
io.imshow(img)
plt.figure()
plt.show(plt.hist(img.flatten(),bins=256))
```



The image redrose.jpg and its histogram

Histograms (cont.)

- The following image is the image which has only three grey levels. (0, 128 and 255)

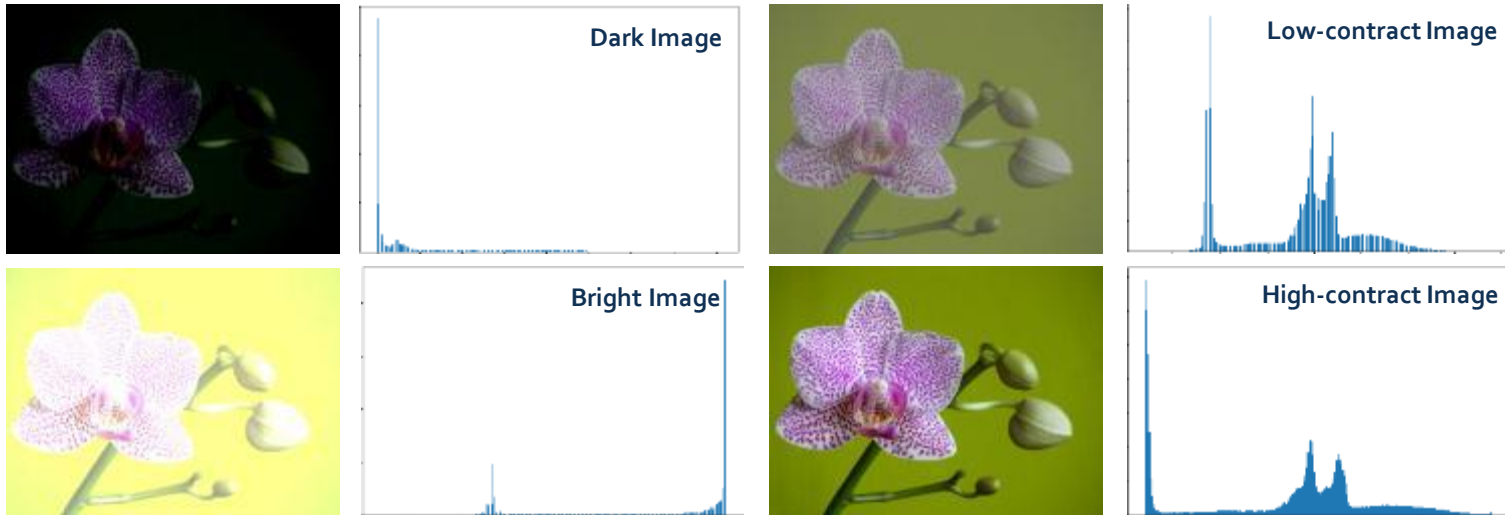


Original image and its histogram

Histograms (cont.)

- ❑ In a **dark image**, the grey levels (and hence the histogram) would be **clustered at the lower end**:
- ❑ In a **uniformly bright image**, the grey levels would be **clustered at the upper end**:
- ❑ In a **low contracted image**, the grey levels would be **clustered together in the centre** of the histogram
- ❑ In a **well contrasted image**, the grey levels would be well spread out over much of the range:

Histograms (cont.)



x-axis – values of intensities
y-axis – their frequencies

Histograms (cont.)

- ❑ Given a poorly contrasted image, we would like to **enhance its contrast, by spreading out its histogram**. There are **two ways** of doing this.
 - ❑ Histogram stretching (Contrast stretching)
 - ❑ Histogram equalization

Histogram stretching (Contrast stretching)

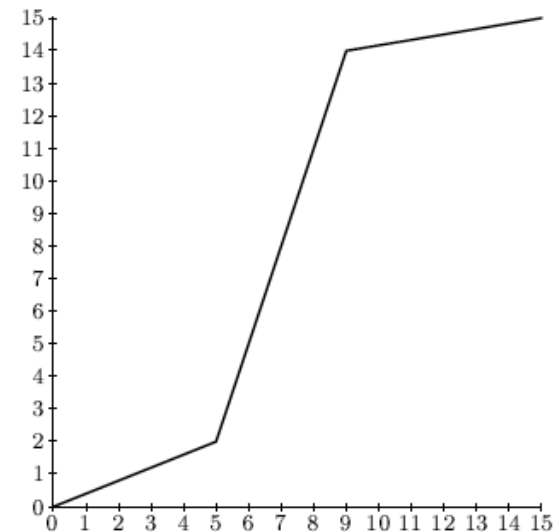
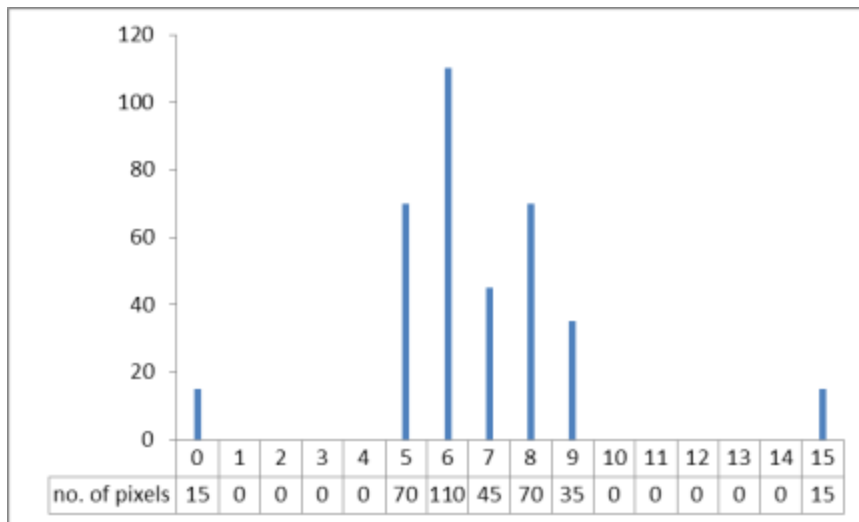
- We have a **low contrast image** with the histogram shown as below, associated with a table of the numbers n_i of grey values:

Grey level i	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
n_i	15	0	0	0	0	70	110	45	70	35	0	0	0	0	0	15

- We can stretch the grey levels in **the centre** of the range out by applying the **piecewise linear function**.
- This function has the effect of stretching the grey levels **5-9** to grey levels **2-14** according to the equation where i is the **original grey level** and j its **result after the transformation**

$$j = \frac{14 - 2}{9 - 5} (i - 5) + 2$$

Histogram stretching (Contrast stretching)



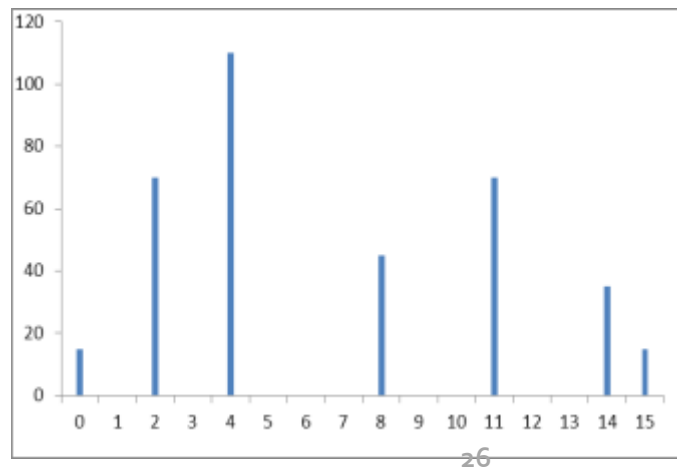
A histogram of a poorly contrasted image, and a stretching function

Histogram stretching (Contrast stretching)

- ❑ Grey levels outside this range are either left alone or transformed according to the linear functions at the ends of the graph above.
- ❑ This yields:

i	5	6	7	8	9
j	2	5	8	11	14

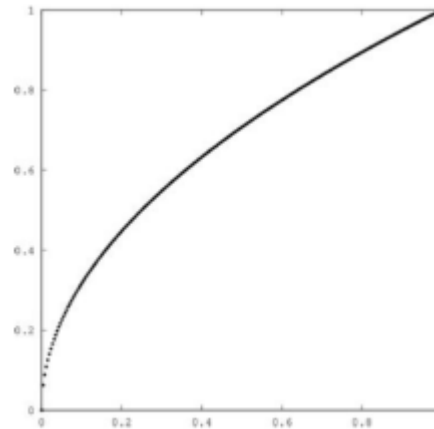
- ❑ The corresponding histogram indicates an image with greater contrast than the original.



Histogram stretching (Contrast stretching)

- + To perform **histogram stretching** in Python the **exposure module of skimage** method may be used.

```
import matplotlib.pyplot as plt
import skimage.io as io
import skimage.exposure as ex
import numpy as np
img=io.imread('images/rice.tif');
plt.figure()
io.imshow(img)
img1=ex.adjust_gamma(img,0.5)
plt.figure()
io.imshow(img1)
```



The function used in above code

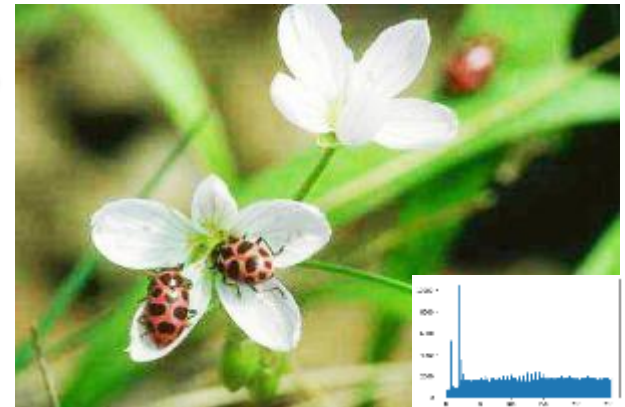
Histogram equalization

- ❑ Histogram stretching **requires user input**.
- ❑ **Histogram equalization** is an entirely **automatic procedure**.
- ❑ The idea is to change the histogram to one which is **uniform**; that is that **every bar** on the histogram is of the **same height**, i.e. each grey level in the image occurs with the **same frequency**.
- ❑ Histogram equalization is used to **adjust the contrast and brightness** of the image.

Histogram equalization (cont.)



Low Contrast



High Contrast

Histogram equalization (cont.)

- Suppose our image has L different grey levels $0, 1, 2, \dots, L-1$, and that grey level i occurs n_i times in the image. Suppose also that the total number of pixels in the image is n

$$n_0 + n_1 + n_2 + \dots + n_{L-1} = n.$$

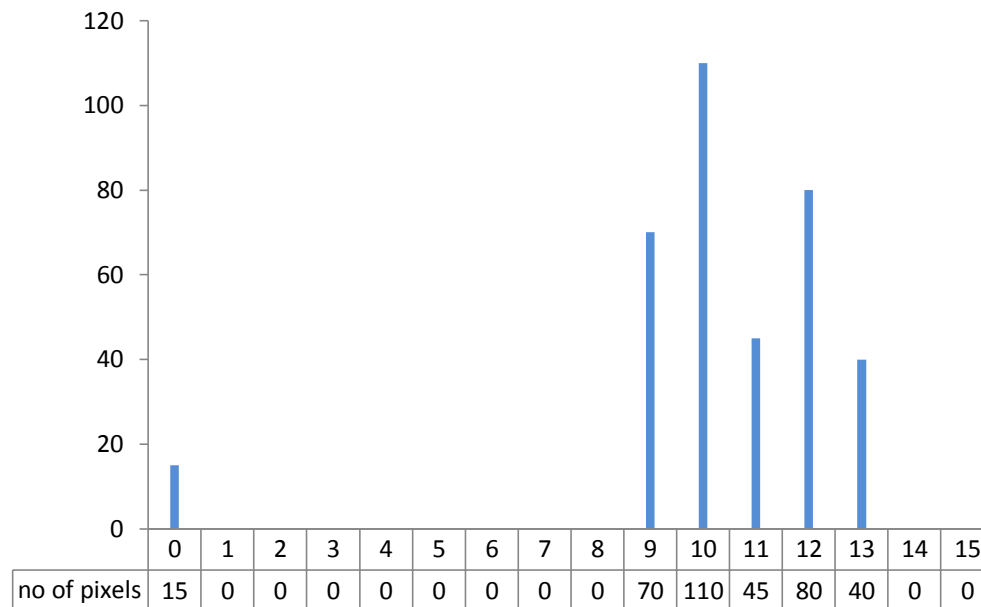
- To transform the grey levels to obtain a better contrasted image, we change grey level i to

$$\frac{(n_0 + n_1 + \dots + n_i)}{n} (L - 1)$$

- And this number is rounded to the nearest integer .

Histogram equalization (cont.)

- Suppose a 4-bit greyscale image has the histogram indicating **poor contrast**.



Histogram equalization (cont.)

Grey Level i	n_i	$\sum n_i$	$(1/24)\sum n_i$	Rounded value
0	15	15	0.63	1
1	0	15	0.63	1
2	0	15	0.63	1
3	0	15	0.63	1
4	0	15	0.63	1
5	0	15	0.63	1
6	0	15	0.63	1
7	0	15	0.63	1
8	0	15	0.63	1
9	70	85	3.65	4
10	110	195	8.13	8
11	45	240	10	10
12	80	320	13.33	13
13	40	360	15	15
14	0	360	15	15
15	0	360	15	15

Histogram equalization (cont.)

Original grey level i	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Final grey level j	1	1	1	1	1	1	1	1	1	4	8	10	13	15	15	15

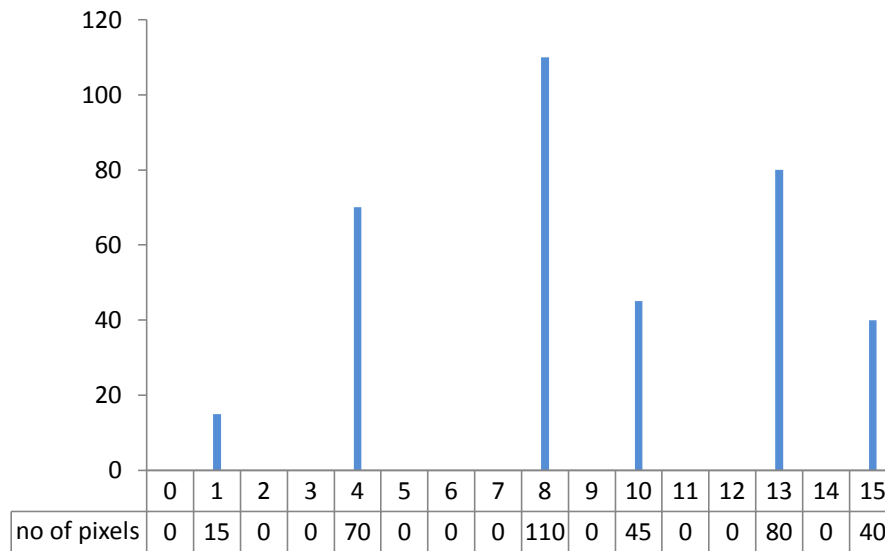


Figure 3. The histogram of figure after equalization

Histogram equalization (cont.)

- ❑ To apply histogram equalization in Python, use the **equalize_hist** function of **skimage.exposure**; for example:

```
img=io.imread('images/rice.tif');  
img1=ex.equalize_hist(img)  
plt.figure()  
io.imshow(img1)  
plt.figure()  
plt.show(plt.hist(img1.flatten(),bins=256))
```

- ❑ Applies histogram equalization to the low contract image, and produces the resulting histogram.

Histogram Equalization (cont.)



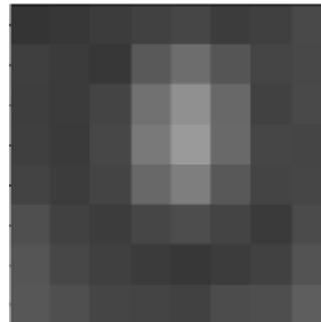
Left column: original images.

Center column: corresponding histogram equalized images.

Right column: histograms of the images in the center column

Histogram Equalization (cont.)

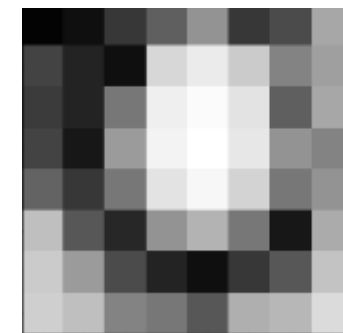
52	55	61	66	70	61	64	73
63	59	55	90	109	85	69	72
62	59	68	113	144	104	66	73
63	58	71	122	154	106	70	69
67	61	68	104	126	88	68	70
79	65	60	70	77	68	58	75
85	71	64	59	55	61	65	83
87	79	69	68	65	76	78	94



8 x 8 small gray image



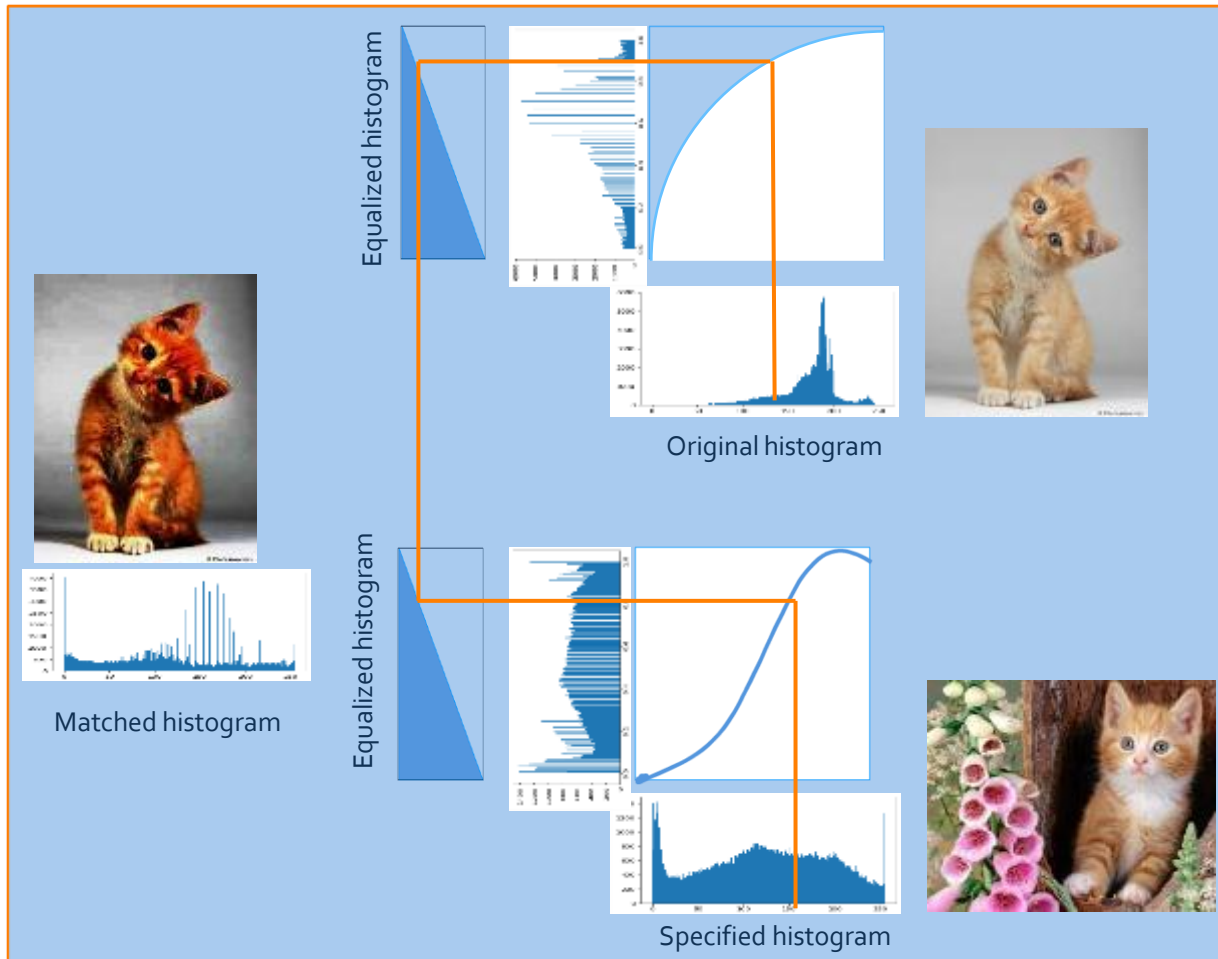
3	15	55	95	147	55	75	167
67	35	15	215	235	203	131	159
59	35	119	239	251	227	95	167
67	23	155	243	255	231	147	131
99	55	119	227	247	211	119	147
191	87	39	147	179	119	23	171
203	155	75	35	15	55	87	195
207	191	131	119	87	175	183	219



Histogram equalized image

```
import skimage.exposure as ex
import numpy as np
import skimage.io as io
img=np.array([[52,55,61,66,70,61,64,73],
             [63,59,55,90,109,85,69,72],
             [62,59,68,113,144,104,66,73],
             [63,58,71,122,154,106,70,69],
             [67,61,68,104,126,88,68,70],
             [79,65,60,70,77,68,58,75],
             [85,71,64,59,55,61,65,83],
             [87,79,69,68,65,76,78,94]])
imgnew=np.uint8(ex.equalize_hist(img)*255)
```

Histogram Matching or Specification



Histogram matching or histogram specification

- ❑ The transformation of an image so that its histogram matches a specified histogram of target image.
- ❑ The idea is to calculate equalized histograms of input and specified images.
- ❑ Do mapping from original histogram to specified histogram through equalized histogram.

Histogram Matching or Specification(cont.)

- Perform the Histogram Matching

Original Image

Grey level	0	1	2	3	4	5	6	7
No. of Pixels	8	10	10	2	12	16	4	2

Desired Image

Grey level	0	1	2	3	4	5	6	7
No. of Pixels	0	0	0	0	20	20	16	8

Histogram Matching or Specification(cont.)

□ Histogram Equalization (Input Image)

Grey level	No. of Pixels (n_k)	PDF (n_k/N)	CDF	(L-1)*CDF	H_k
0	8	0.13	0.13	0.91	1
1	10	0.16	0.29	2.03	2
2	10	0.16	0.45	3.15	3
3	2	0.03	0.48	3.36	3
4	12	0.18	0.66	4.62	5
5	16	0.25	0.91	6.37	6
6	4	0.06	0.97	6.79	7
7	2	0.03	1.0	7	7

64

1

Histogram Matching or Specification(cont.)

□ Histogram Equalization (Target Image)

Grey level	No. of Pixels (n_k)	PDF (n_k/N)	CDF	$(L-1)*CDF$	S_k
0	0	0	0	0	0
1	0	0	0	0	0
2	0	0	0	0	0
3	0	0	0	0	0
4	20	0.31	0.31	2.17	2
5	20	0.31	0.62	4.34	4
6	16	0.25	0.87	6.09	6
7	8	0.13	1.0	7	7
	64	1			

Histogram Matching or Specification(cont.)

□ Mapping

Grey Scale	H	S	Map
0	1	0	4
1	2	0	4
2	3	0	5
3	3	0	5
4	5	2	6
5	6	4	6
6	7	6	7
7	7	7	7

Original grey level i	0	1	2	3	4	5	6	7
Final grey level j	4	4	5	5	6	6	7	7

Histogram Matching or Specification(cont.)

Modified Image

Grey Level	0	1	2	3	4	5	6	7
No. of Pixels	0	0	0	0	18	12	28	6

0	0	0	1	2	4	5	5
0	0	1	1	2	4	5	5
0	0	1	1	2	4	5	6
0	1	1	2	2	4	5	6
1	1	1	2	3	4	5	6
2	2	2	2	3	4	5	6
4	4	4	4	4	4	5	7
5	5	5	5	5	5	5	7

Input Image

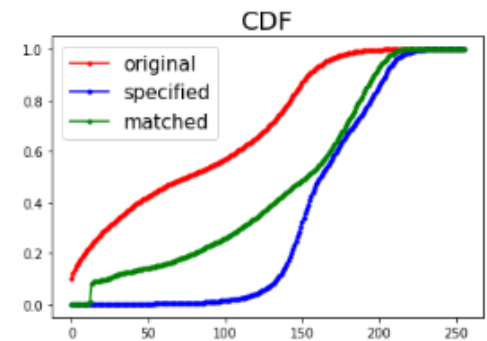
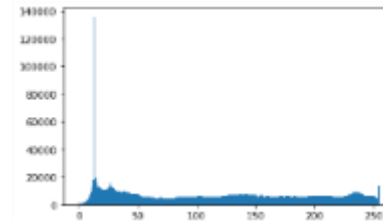
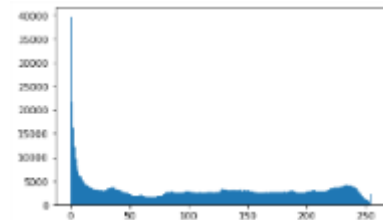
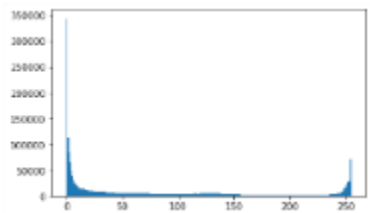
4	4	4	4	5	6	6	7
4	4	4	4	5	6	6	7
4	4	5	5	5	6	6	7
4	4	5	5	5	6	6	7
4	4	5	5	5	6	6	7
4	4	5	5	5	6	6	7
4	4	5	5	5	6	6	7
4	4	5	5	5	6	6	7

Target Image

4	4	4	4	5	6	6	6
4	4	4	4	5	6	6	6
4	4	4	4	5	6	6	7
4	4	4	5	5	6	6	7
4	4	4	5	5	6	6	7
5	5	5	5	5	6	6	7
6	6	6	6	6	6	6	7
6	6	6	6	6	6	6	7

Modified Image

Histogram Matching or Specification(cont.)



- First column : original images and its histogram.
- Second column : specified image and its histogram.
- Third column : matched image and its histogram.
- Fourth column : cumulative distribution of images

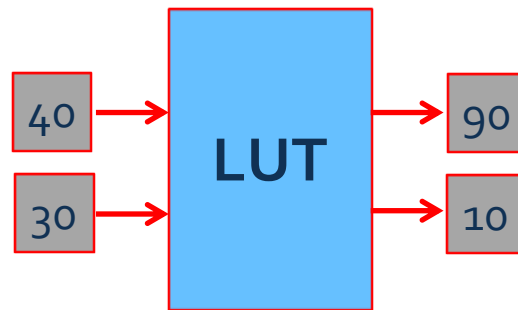
Lookup tables

- ❑ **Point operations** can be performed very effectively by the use of a **lookup table**, known more simply as an **LUT**.
- ❑ For operating on images of type uint8, such a table consists of a **single array of 256 values**, each value of which is an integer in the **range 0...255**.
- ❑ Then our operation can be implemented by **replacing each pixel value by the corresponding value** in the table.

Lookup tables (cont.)

40	40	40	40
40	30	30	40
40	30	30	40
40	40	40	40

Low Contract



90	90	90	90
90	10	10	90
90	10	10	90
90	90	90	90

High Contract

Contract is changed by changing pixel values.

Lookup tables (cont.)

- ❑ LUT corresponding to **division by 2** can be reconstructed:

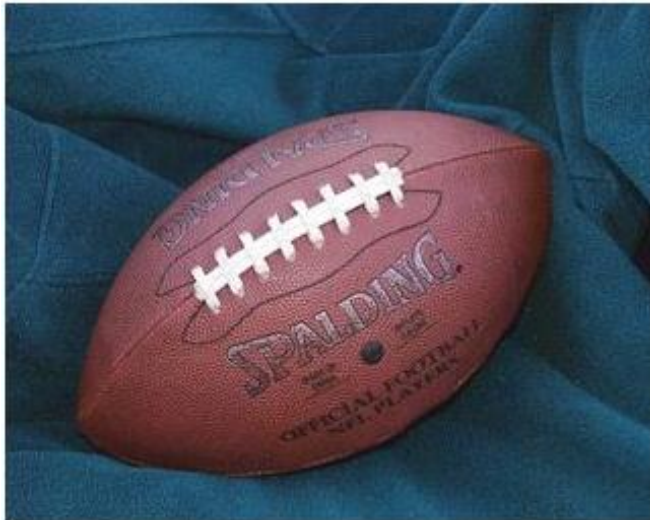
Index	0	1	2	...	252	253	254	255
LUT	0	0	1	...	125	126	127	127

- ❑ A pixel with **value 2** will be replaced with **1**; a pixel with **value 253** will be replaced with value **126**.
- ❑ The above lookup table (division by 2) can be applied by the simple command **T[im]** in Python ,i.e. **T** is **lookup table** and **im** is input image.

```
T=np.uint8(np.arange(256))/2  
img1=np.uint8(T[img])
```

Lookup tables (cont.)

```
T=np.uint8(np.arange(256))/2  
img=io.imread('football.jpg');  
plt.figure()  
io.imshow(img)  
img1=np.uint8(T[img])  
plt.figure()  
io.imshow(img1)
```



original image



Image using LUT table

Lookup tables (cont.)

□ Contrast stretching function

- Create a LUT to implement the contrast stretching function shown in figure. Givens are the equations of the three lines used for lookup table.

$$y = \frac{64}{96}x$$

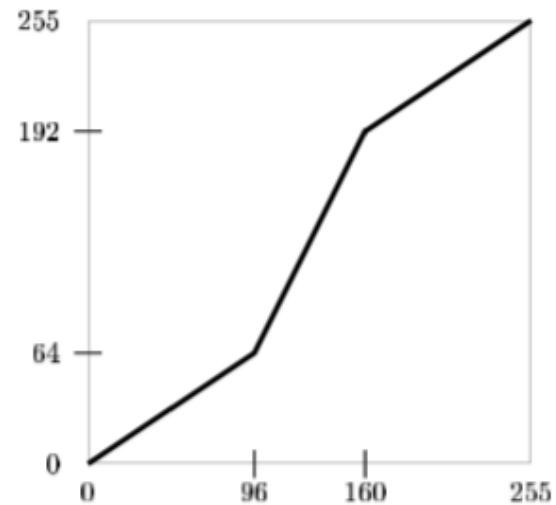
$$y = \frac{192 - 64}{160 - 96}(x - 96) + 64$$

$$y = \frac{255 - 192}{255 - 160}(x - 160) + 192$$

$$y = 0.6667x$$

$$y = 2x - 128$$

$$y = 0.6632x + 85.8947$$

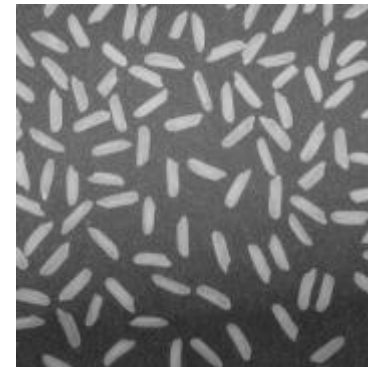


Contract stretching function

Lookup tables (cont.)

□ Python code for contrast stretching function

```
import matplotlib.pyplot as plt
import skimage.io as io
import numpy as np
#create table for contrast stretching function
t1=np.uint8(np.arange(97))*0.6667
t2=2*np.uint8(np.arange(97,161))-128
t3=0.6632*np.uint8(np.arange(161,256))+85.8947
T=np.concatenate((t1,t2,t3))
# apply table to image
img=io.imread('images/rice.tif');
plt.figure()
io.imshow(img)
img1=np.uint8(T[img])
plt.figure()
io.imshow(img1)
```



Original Image

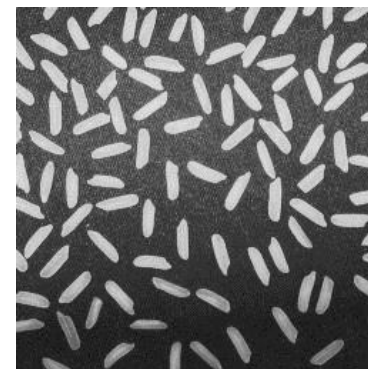


Image using LUT table

Assignment

The following small image has grey values in the range 0 to 15. Compute the grey level histogram and the mapping that will equalize this histogram. Produce an 8x8 grid containing the grey values for the new histogram-equalized image.

11	3	2	12	15	15	17	15
9	7	5	2	5	9	15	15
6	5	1	1	4	11	18	19
7	4	1	0	7	11	12	17
17	6	12	12	17	19	19	17
11	7	15	15	18	18	17	15
9	5	7	11	15	12	15	15
5	3	1	4	6	9	11	11

Assignment (cont.)

The following small image has grey values in the range 0 to 7. Perform histogram matching for image₁ to match histogram of desired image₂. Produce an 8x8 grid containing the grey values for the new histogram-specified image.

0	1	5	2	4	3	5	5
5	5	1	2	3	4	5	5
1	0	2	0	4	4	4	6
1	1	4	2	2	4	5	6
4	4	1	0	2	0	5	5
4	1	1	2	0	5	5	5
4	1	0	0	2	5	6	7
4	1	2	2	5	5	7	6

Image 1

4	7	5	5	5	5	6	6
5	4	4	4	5	4	6	6
5	5	4	5	4	5	5	7
5	4	4	4	5	4	6	7
5	4	4	4	5	4	6	7
5	5	4	4	5	4	6	7
5	6	6	6	4	4	6	7
5	6	6	6	6	6	7	7

Image 2

Python code

```
##histogram equalization for gray image##
import numpy as np
from matplotlib import pyplot as plt
from skimage.color import rgb2gray
import skimage.io as io
img=io.imread('images/lowcontractflowers.jpg')
img=np.int32(255*rgb2gray(img))
imgnew=img.copy()
l,w=img.shape
n=l*w
L=img.max()
bin=np.zeros(L+1)
binnew=np.zeros(L+1)
for i in range(l):
    for j in range(w):
        for k in range(L+1):
            if img[i][j]==k:
                bin[k]=bin[k]+1
for k in range(L+1):
    binnew[k]=(np.sum(bin[0:k+1]))*(L/n).round()
for i in range(l):
    for j in range(w):
        for k in range(L+1):
            if imgnew[i][j]==k:
                imgnew[i][j]=binnew[k]
                break
```

Python code (cont.)

```
def goto(line) :
    global lineNumber
    lineNumber=line

def find_hist_eq(img,L):
    l,w=img.shape
    n=l*w
    L=img.max()
    bin=np.zeros(L+1)
    binnew=np.zeros(L+1)
    for i in range(l):
        for j in range(w):
            for k in range(L+1):
                if img[i][j]==k :
                    bin[k]=bin[k]+1
    for k in range(L+1):
        binnew[k]=(np.sum(bin[o:k+1])*(L/n)).round()
    return binnew
```

```
## Histogram Matching ###
from skimage import data
img1= data.coffee()
img2 = data.chelsea()
imgnew=img1.copy()
l,w=img1.shape
L1=img1.max()
L2=img2.max()
bin1=np.zeros(L1+1)
bin2=np.zeros(L2+1)
bin3=np.zeros(L2+1)
bin1=find_hist_eq(img1,L1)
bin2=find_hist_eq(img2,L2)
j=0
i=0
c=L1
while i <=c:
    while j <= 7:
        if bin1[i]==bin2[j]:
            bin3[i]=j
            break
        j=j+1
    if j==8:
        bin1[i]=bin1[i]+1
        j=0
        i-=1
        goto(41)
    i=i+1
```

```
for p in range(8):
    for q in range(8):
        for r in range(8):
            if imgnew[p][q]==r :
                imgnew[p][q]=bin3[r]
            break
```

Next Week Lecture (Week3)

- Lecture3:Image Enhancement in Spatial Domain (Neighborhood Processing)

Thank You